## Exercise 8

Parts 1 to 12 have to be produced on 6 machines A; B, C, D, E, and F.

|  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | 1 | 1 | 1 | 1 | 1 |  |  |  |  |  |  | 1 |
| B | 1 |  |  |  |  |  | 1 | 1 | 1 | 1 |  |  |
| C | 1 | 1 | 1 | 1 | 1 |  |  |  |  |  | 1 |  |
| D |  |  |  |  |  | 1 | 1 | 1 | 1 | 1 | 1 |  |
| E |  | 1 | 1 | 1 | 1 | 1 |  |  |  |  |  |  |
| F |  |  |  |  |  | 1 | 1 | 1 | 1 | 1 |  | 1 |

a) Show that this yields the following graph of common parts:

b) Assume that the graph of common parts is as given above. Let the initial clustering of machines in 2 groups be $\{\mathrm{A}, \mathrm{B}, \mathrm{C}\}$ and $\{\mathrm{D}, \mathrm{E}, \mathrm{F}\}$. Using the Kerninghan-Lin algorithm find an improved clustering of the 6 machines in 2 groups.

## Excercise 9

Fort he final assembly of a product 10 jobs need to be done (A, B, ..., J). The following table contains the processing times (in minutes) and precedence conditions for all jobs.

| Job | Precedessor | Proc.time |
| :---: | :---: | :---: |
| A | - | 7 |
| B | - | 8 |
| C | - | 7 |
| D | A, B | 6 |
| E | C, D | 12 |
| F | D | 8 |
| G | E | 10 |
| H | E | 12 |
| I | F, H | 8 |
| J | G, H | 9 |

a) Determine the cyle time if production is done in 2 working shifts, each of them taking 8 hours, and an output quantity of 50 items.
b) Apply the following priority rules for assigning jobs to stations (apply rule 1 first, rule 2 is only to be applied in case of equality obtained with rule 1

Rule 1: Choose jobs according to monotonuously increasing upper bound for the number of stations needed for job j and all his precedessors.

$$
\mathrm{PV}_{\mathrm{j}}:=\mathrm{E}_{\mathrm{j}}=\left\lceil\left(t_{j}+\sum_{h \in V_{j}^{m}} t_{h}\right) / c\right\rceil
$$

Rule 2: Decreasing positional weight („Positionswert")
c) Calculate the system's efficiency.

## Exercise 10

Models A, B and C are to be produced by mixed-model assembly. The following table contains the precedence conditions and processing times for all jobs of all models:

|  | A |  | B |  | C |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Job | Precedessor | $\mathrm{t}_{\mathrm{jA}}$ | Precedessor | $\mathrm{t}_{\mathrm{j} \mathrm{B}}$ | Precedessor | $\mathrm{t}_{\mathrm{jC}}$ |
| a | - | 4 | - | 3 | - | 1 |
| b | a | 7 | a | 1 | - | 3 |
| c | a | 2 | d | 2 | d | 3 |
| d | a | 1 | - | 5 | a | 2 |
| e | $\mathrm{b}, \mathrm{d}$ | 5 | $\mathrm{~b}, \mathrm{c}$ | 2 | a | 1 |
| f | $\mathrm{c}, \mathrm{e}$ | 1 | e | 4 | $\mathrm{~b}, \mathrm{c}, \mathrm{e}$ | 3 |

We have to produce 3 units of model A, 1 unit of model B, and 2 units of model C. The planning horizon is 60 time units.
a) Assign jobs to stations by applying the heuristic of Thomopoulos $(\lambda=0)$.
b) Assume $\lambda$ to be 20. Does the solution found in a) change?

## Exercise 11

Models A, B and C are to be produced by mixed-model assembly. The following table contains the precedence conditions and processing times for all jobs of all models:

|  | A |  | B |  | $C$ |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Job | Pred. | $\mathrm{t}_{\mathrm{j} A}$ | Pred. | $\mathrm{t}_{\mathrm{jB}}$ | Pred. | $\mathrm{t}_{\mathrm{j} \mathrm{C}}$ |
| a | - | 2 | - | 3 | - | 2 |
| b | a | 3 | a | 2 | a | 2 |
| c | - | - | a | 2 | a | 1 |
| d | b | 4 | a | 6 | a | 1 |
| e | b | 6 | - | - | $\mathrm{b}, \mathrm{c}$ | 2 |
| f | $\mathrm{e}, \mathrm{d}$ | 2 | $\mathrm{~b}, \mathrm{c}, \mathrm{d}$ | 2 | $\mathrm{~d}, \mathrm{e}$ | 1 |

We have to produce 1 unit of model A, 2 units of model B, and 2 units of model C. The planning horizon is 40 time units.
a) Assign jobs to stations by applying the heuristic of Thomopoulos $(\lambda=0)$.
b) What happens if $\lambda$ is assumed to be 34 ?

## Exercise 12

Consider the following precedence graph for an assembly line. The numbers above the nodes (operations) indicate the durations.

a) What is the minimal possible cycle time, if exactly 2 stations should be built. Explain why!
b) Let the cycle time be $\mathrm{c}=5$. Find the optimal assembly line balancing using dynamic programming (Jackson).

