Transportation Logistics

# Part VI: VRP - improvement heuristics

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VRP - improvement heuristics

A classification

Intra-route (single-route)

Improvement heuristics working on a single route (all TSP operators!)

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Inter-route (multiroute)

Improvement heuristics considering several routes at once.

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 $\lambda$  edges are removed from the tour and the  $\lambda$  remaining segments are reconnected in all possible ways (2-opt, 3-opt...)

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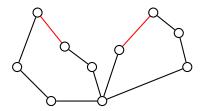
#### 4-opt\* (Renaud et al., 1996)

a restricted version of 4-opt: promising reconnections between a sequence of at most w edges and another sequence of 2 edges.

(Following Van Breedam's classification)

## String cross

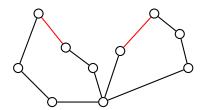
Two strings of vertices are exchanged by crossing two edges in two different routes. (2-opt\*: two edges from different routes are replaced by two new edges)

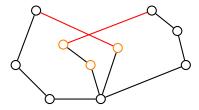


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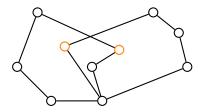


Source: Laporte and Semet (2002) Classical Heuristics for the CVRP. Chapter 5 of Paolo Toth, and Daniele Vigo (eds) The Vehicle Routing Problem, SIAM.

(Following Van Breedam's classification)

String exchange (swap)

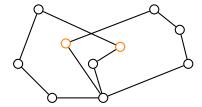
Two strings of at most k vertices are exchanged between two routes.

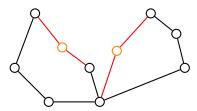


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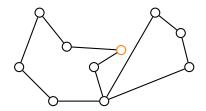
Source: Laporte and Semet (2002) Classical Heuristics for the CVRP. Chapter 5 of Paolo Toth, and Daniele Vigo (eds) The Vehicle Routing Problem, SIAM.

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## String relocation (move)

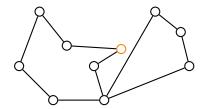
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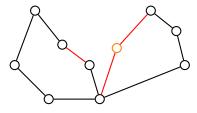


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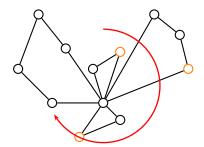




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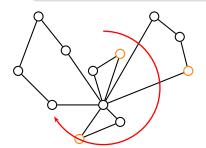
#### Cyclic transfer

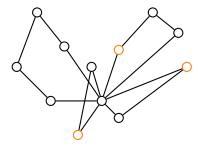
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good vs. bad starting solution

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 vs.  $k = 2$ 

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## References

Paolo Toth, and Daniele Vigo (2002) The Vehicle Routing Problem, SIAM. (Chapter 5)

W. Domschke (1997) 'Logistik: Rundreisen und Touren' Oldenbourg.